

Stats Exam 2 Formula Sheet

Confidence Intervals:

$$CI = \bar{x} \pm t_{\alpha} \left(\frac{s}{\sqrt{n-1}} \right) \quad CI = \bar{x} \pm z_{\alpha} \left(\frac{s}{\sqrt{n-1}} \right)$$

$$CI = \hat{p} \pm z_{\alpha} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Chi-Square:

$$df = (r-1)(c-1)$$

$$\chi^2_{\text{obt}} = \sum \frac{(f_{oi} - f_{ei})^2}{f_{ei}}$$

$$f_{ei} = \frac{r_{mi} \cdot c_{mi}}{n}$$

Cramer's V:

$$V = \sqrt{\frac{\chi^2_{\text{obt}}}{n \cdot m}}$$

T test: Independent-Samples, Pooled Variances:

$$df = N_1 + N_2 - 2$$

$$\hat{\sigma}_{\bar{x}_1 - \bar{x}_2} = \sqrt{\frac{(N_1-1)s_1^2 + (N_2-1)s_2^2}{N_1 + N_2 - 2}} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}$$

$$t_{\text{obt}} = \frac{\bar{x}_1 - \bar{x}_2}{\hat{\sigma}_{\bar{x}_1 - \bar{x}_2}}$$

T test: Independent-Samples, Separate Variances:

$$df = \frac{\left(\frac{s_1^2}{N_1} + \frac{s_2^2}{N_2} \right)^2}{\left(\frac{s_1^2}{N_1} \right)^2 \left(\frac{1}{N_1-1} \right) + \left(\frac{s_2^2}{N_2} \right)^2 \left(\frac{1}{N_2-1} \right)}$$

$$\hat{\sigma}_{\bar{x}_1 - \bar{x}_2} = \sqrt{\frac{s_1^2}{N_1-1} + \frac{s_2^2}{N_2-1}}$$

$$t_{\text{obt}} = \frac{\bar{x}_1 - \bar{x}_2}{\hat{\sigma}_{\bar{x}_1 - \bar{x}_2}}$$

T test: Dependent Samples:

$$df = N_{\text{pairs}} - 1$$

$$x_0 = x_1 - x_2 \quad \bar{x}_0 = \text{mean of } x_0$$

$$\bar{x}_0 = \frac{\sum x_0}{N}$$

$$SD = \sqrt{\frac{\sum (x_0 - \bar{x}_0)^2}{N_{\text{pairs}} - 1}}$$

$$\hat{\sigma}_{\bar{x}_1 - \bar{x}_2} = \frac{SD}{\sqrt{N_{\text{pairs}}}}$$

$$t_{\text{obt}} = \frac{\bar{x}_0}{\hat{\sigma}_{\bar{x}_1 - \bar{x}_2}}$$

T test: Proportions:

$$\hat{q} = 1 - \hat{p} \quad \hat{p} = \frac{N_1 \hat{p}_1 + N_2 \hat{p}_2}{N_1 + N_2}$$

$$\hat{\sigma}_{\hat{p}_1 - \hat{p}_2} = \sqrt{\hat{p}\hat{q}} \sqrt{\frac{N_1 + N_2}{N_1 N_2}}$$

$$z_{\text{obt}} = \frac{\hat{p}_1 - \hat{p}_2}{\hat{\sigma}_{\hat{p}_1 - \hat{p}_2}}$$

ANOVA:

$$df_B = k - 1 \quad df_W = N - k$$

* 7-step process:

1) Find the sum of each group, each group's mean, and the grand mean. $\sum x_k$
 $\bar{x}_k = \frac{\sum_i \sum_k x}{N}$

2) Find the sum of each group's squared raw scores.
 $\sum x_k^2$

3) Compute the total Sum of Squares.

$$SS_T = \sum_i \sum_k x^2 - \frac{(\sum_i \sum_k x)^2}{N}$$

4) Compute the between-group Sum of Squares.

$$SS_B = n_1 (\bar{x}_1 - \bar{x}_G)^2 + n_2 (\bar{x}_2 - \bar{x}_G)^2 + n_3 (\bar{x}_3 - \bar{x}_G)^2$$

do this for each group (may have more than 3)

ANOVA Continued:

5) Compute the within-group Sum of Squares.

$$SS_w = SS_T - SS_B$$

6) Find the Mean Squares.

$$MS_B = \frac{SS_B}{k-1} \quad MS_w = \frac{SS_w}{N-k}$$

7) Calculate $F_{obtained}$.

$$F_{obt} = \frac{MS_B}{MS_w}$$

Omega Squared:

$$\omega^2 = \frac{SS_B - (k-1)MS_w}{MS_w + SS_T}$$

Correlations:

$$df = N - 2 \quad \text{no } N \text{ here (my mistake!)}$$

$$r = \frac{N \sum xy - \sum x \sum y}{\sqrt{[N \sum x^2 - (\sum x)^2][N \sum y^2 - (\sum y)^2]}}$$

$$t_{obt} = r \sqrt{\frac{N-2}{1-r^2}}$$

Coefficient of Determination: r^2

Sign: is r negative or positive?

Magnitude: how large is r ? Is it indicating a weak, moderate, strong or very strong relationship?